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Temporal networks

Temporal quantities Operations

# Analysis of Peer Review data from WoS 

# part 4: an approach to temporal analysis 

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## PEERE

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## PRERE Outline

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## Temporal

 networksTemporal quantities

Operations
Bibliographic temporal networks

Conclusions

1 Temporal networks
2 Temporal quantities
3 Operations
4 Bibliographic temporal networks
5 Conclusions


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## Temporal

networks
Temporal
quantities
Operations

## Bibliographic

temporal
networks
Conclusions

## Work in progress

Temporal networks / paper

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A. Ferligoj

Temporal networks

Temporal quantities

Operations
Bibliographic temporal networks

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ORIGINAL ARTICLE

## An algebraic approach to temporal network analysis based on temporal quantities

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Abstract In a temporal network, the presence and activity of nodes and links can change through time. To describe temporal networks we introduce the notion of temporal

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## Temporal networks

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Temporal networks

Temporal quantities

A temporal network $\mathcal{N}_{T}=(\mathcal{V}, \mathcal{L}, \mathcal{P}, \mathcal{W}, \mathcal{T})$ is obtained by attaching the time, $\mathcal{T}$, to an ordinary network where $\mathcal{T}$ is a set of time points, $t \in \mathcal{T}$.

In a temporal network, nodes $v \in \mathcal{V}$ and links $I \in \mathcal{L}$ are not necessarily present or active in all time points. Let $T(v), T \in \mathcal{P}$, be the activity set of time points for node $v$ and $T(I), T \in \mathcal{W}$, the activity set of time points for link $/$.

Besides the presence/absence of nodes and links also their properties can change through time.

## Temporal quantities

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Temporal quantities Operations

We introduce a notion of a temporal quantity

$$
a(t)= \begin{cases}a^{\prime}(t) & t \in T_{a} \\ \nsim & t \in \mathcal{T} \backslash T_{a}\end{cases}
$$

where $T_{a}$ is the activity time set of $a$ and $a^{\prime}(t)$ is the value of $a$ in an instant $t \in T_{a}$, and $\mathscr{H}$ denotes the value undefined.

We assume that the values of temporal quantities belong to a set $A$ which is a semiring $(A,+, \cdot, 0,1)$ for binary operations $+: A \times A \rightarrow A$ and $\cdot: A \times A \rightarrow A$.
We can extend both operations to the set $A_{\mathscr{H}}=A \cup\{\mathscr{H}\}$ by requiring that for all $a \in A_{\mathscr{H}}$ it holds

$$
a+\mathscr{H}=\mathscr{H}+a=a \quad \text { and } a \cdot \mathscr{H}=\mathscr{H} \cdot a=\mathscr{H} .
$$

The structure $\left(A_{\mathscr{H}},+, \cdot, \mathscr{H}, 1\right)$ is also a semiring.

## Semiring addition and multiplication in networks.

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Temporal networks

Temporal quantities

The "default" semiring is the combinatorial semiring $\left(\mathbb{R}_{0}^{+},+, \cdot, 0,1\right)$ where + and $\cdot$ are the usual addition and multiplication of real numbers.


In applications of semirings in analysis of graphs and networks the addition + describes the composition of values on parallel paths and the multiplication • describes the composition of values on sequential paths. For a combinatorial semiring these two schemes correspond to basic principles of combinatorics Rule of Sum and Rule of Product.

## Operations with temporal quantities

Let $A_{\mathscr{H}}(\mathcal{T})$ denote the set of all temporal quantities over $A_{\mathscr{H}}$ in time $\mathcal{T}$. To extend the operations to networks and their matrices we first define the sum (parallel links) $a+b$ as

$$
(a+b)(t)=a(t)+b(t) \quad \text { and } \quad T_{a+b}=T_{a} \cup T_{b}
$$

The product (sequential links) $a \cdot b$ is defined as

$$
(a \cdot b)(t)=a(t) \cdot b(t) \quad \text { and } \quad T_{a \cdot b}=T_{a} \cap T_{b} .
$$

Let us define the temporal quantities $\mathbf{0}$ and $\mathbf{1}$ with requirements $\mathbf{0}(t)=\mathscr{H}$ and $\mathbf{1}(t)=1$ for all $t \in \mathcal{T}$. Again, the structure $\left(A_{\mathscr{H}}(\mathcal{T}),+, \cdot, \mathbf{0}, \mathbf{1}\right)$ is a semiring.

## Semiring for temporal quantities

A semiring is also the set of square matrices of order $n$ over it for addition $\mathbf{A} \oplus \mathbf{B}=\mathbf{S}$

$$
s_{i j}=a_{i j}+b_{i j}
$$

and multiplication $\mathbf{A} \odot \mathbf{B}=\mathbf{P}$

$$
p_{i j}=\sum_{k=1}^{n} a_{i k} \cdot b_{k j} .
$$

The matrix multiplication is closely related to traveling on networks. For a value $p_{i j}$ to be defined (different from $\mathscr{H}$ ) there should exist at least one node $k$ such that both link $(i, k)$ and link $(k, j)$ exist (at the same time) - the transition from the node $i$ to the node $j$ through a node $k$ is possible. Its contribution is $a_{i k} \cdot b_{k j}$.

## Temporal quantities on intervals

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Temporal networks

Temporal quantities Operations

In the following we shall limit our discussion to temporal quantities that can be described in the form of time-interval/value sequences

$$
a=\left(\left(l_{i}, v_{i}\right)\right)_{i=1}^{k}
$$

where $I_{i}$ is a time-interval, $T_{a}=\bigcup_{i=1}^{k} I_{i}$, and $v_{i}$ is a constant value of $a$ on this interval. To simplify the exposition we will assume in the following that all the intervals are of the form $\left[s_{i}, f_{i}\right), s_{i}$ is the starting time and $f_{i}$ is the finishing time. Therefore we can describe the temporal quantities with sequences

$$
a=\left(\left(s_{i}, f_{i}, v_{i}\right)\right)_{i=1}^{k}
$$

To provide a computational support for the proposed approach we are developing in Python a library TQ (Temporal Quantities). The following are two temporal quantities $a$ and $b$ represented in Python

```
a = [(1, 5, 2), (6, 8, 1), (11, 12, 3), (14, 16, 2),
    (17, 18, 5), (19, 20, 1)]
b = [(2, 3, 4), (4, 7, 3), (9, 10, 2), (13, 15, 5), (16, 21, 1)]
```

The temporal quantity $a$ has on interval $[1,5)$ value 2 , on interval $[6,8)$ value 1 , on interval $[11,12$ ) value 3 , etc. Outside the specified intervals its value is undefined, $\mathscr{H}$.

## Sum and product of temporal quantities

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A. Ferligoj

Temporal networks

Temporal quantities

Operations
Bibliographic temporal networks

$$
\begin{aligned}
& \mathrm{a}=[(1,5,2),(6,8,1),(11,12,3),(14,16,2), \\
& \mathrm{b}=[(2,3,4),(4,7,3),(9,10,2),(13,15,5),(16,21,1)]
\end{aligned}
$$

The following are the sum $s=a+b$ and the product $p=a \cdot b$ of temporal quantities $a$ and $b$ over combinatorial semiring.

$$
\begin{aligned}
s= & {[(1,2,2),(2,3,6),(3,4,2),(4,5,5),(5,6,3),} \\
& (6,7,4),(7,8,1),(9,10,2),(11,12,3), \\
& (13,14,5),(14,15,7),(15,16,2),(16,17,1), \\
& (17,18,6),(18,19,1),(19,20,2),(20,21,1)] \\
p= & {[(2,3,8),(4,5,6),(6,7,3),(14,15,10),} \\
& (17,18,5),(19,20,1)]
\end{aligned}
$$

They are visually displayed at the bottom half of figures on the following slides.

## Addition of temporal quantities.

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## Temporal

networks
Temporal quantities

Operations
Bibliographic
temporal
networks
Conclusions

a:

Multiplication of temporal quantities.

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Temporal
networks
Temporal quantities

Operations
Bibliographic
temporal
networks
Conclusions


## The aggregated value

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Temporal networks

Temporal quantities

Operations
Bibliographic

In some applications over the combinatorial semiring we shall use the aggregated value of a temporal quantity $a=\left(\left(s_{i}, f_{i}, v_{i}\right)\right)_{i=1}^{k}$. It is defined as

$$
\Sigma a=\sum_{i=1}^{k}\left(f_{i}-s_{i}\right) \cdot v_{i}
$$

and is computed using the procedure total. For example $\Sigma a=23$ and $\Sigma b=30$. Note that $\Sigma a+\Sigma b=\Sigma(a+b)$.

## Networks from bibliographic data

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Temporal networks

Temporal quantities

Operations
Bibliographic temporal networks

From special bibliographies (BibTEX) and bibliographic services (Web of Science, Scopus, SICRIS, CiteSeer, Zentralblatt MATH, Google Scholar, DBLP Bibliography, US patent office, and others) we can derive some two-mode networks on selected topics:

- works $\times$ authors (WA),
- works $\times$ keywords (WK);
and from some data also the network
- works $\times$ classification (WC), and the
- one-mode citation network works $\times$ works ( $\mathbf{C i}$ ); where works include papers, reports, books, patents etc.

Besides this we get also at least the partition of works by the journal or publisher and the partition of works by the publication year.

For converting WoS file into networks in Pajek's format a program WoS2Pajek was developed (in Python).

## Temporal co-occurrence networks

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Temporal networks

Temporal quantities

Operations
Bibliographic temporal networks

Let the binary matrix $\mathbf{A}=\left[a_{e p}\right]$ describe a two-mode network on the set of events $E$ and the set of of participants $P$ :

$$
a_{e p}= \begin{cases}1 & p \text { participated in the event } e \\ 0 & \text { otherwise }\end{cases}
$$

The function $d: E \rightarrow \mathcal{T}$ assigns to each event $e$ the date $d(e)$ when it happened. $\mathcal{T}=[$ first, last $] \subset \mathbb{N}$. Using these data we can construct two temporal affiliation matrices:

- instantaneous $\mathbf{A i}=\left[a i_{e p}\right]$, where

$$
a i_{e p}= \begin{cases}{[(d(e), d(e)+1,1)]} & a_{e p}=1 \\ {[]} & \text { otherwise }\end{cases}
$$

- cumulative $\mathbf{A c}=\left[a c_{e p}\right]$, where

$$
a c_{e p}= \begin{cases}{[(d(e), \text { last }+1,1)]} & a_{e p}=1 \\ {[]} & \text { otherwise }\end{cases}
$$

## Example

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## Temporal

 quantitiesOperations
Bibliographic temporal networks

Conclusions

BORNMANN_L (2007) 1:83 Bornmann, L., Daniel, H.-D. (2007). Gatekeepers of science - Effects of external reviewers' attributes on the assessments of fellowship applications. Journal of Informetrics, 1(1), 83-91. DANIEL_H (2007) : 71 Daniel, H.-D., Mittag, S., Bornmann, L. (2007). The potential and problems of peer evaluation in higher education and research. In: A. Cavalli (Ed.), Quality Assessment for Higher Education in Europe (p. 71-82). London, UK: Portland Press.
BORNMANN_L (2007) : 149 Bornmann, L., Daniel, H.-D. (2007). Functional use of frequently and infrequently cited articles in citing publications. A content analysis of citations to articles with low and high citation counts. In Daniel Torres-Salinas, Henk F. Moed (Eds.), Proceedings of the 11th International Conference of the International Society for Scientometrics and Informetrics, 2007 (pp. 149-153). Madrid, Spain: Spanish Research Council (CSIC).
BORNMANn_L(2006) 15:209 Bornmann, L., Daniel, H.-D. (2006). Potential sources of bias in research fellowship assessments. Effects of university prestige and field of study on approval and rejection of fellowship applications. Research Evaluation, 15(3), 209-219.
BORNMANN_L (2006) 20:347 Bornmann, L. (2006). Peer-Review zur Auswahl von Forschungsstipendiaten. Eine Analyse der Fairness und prognostischen Validität des Auswahlprozesses mittels CHAID und GLM. Empirische Pädagogik, 20(4), 347-368.
MITTAG_S (2006) 28:6 Mittag, S., Bornmann, L., Daniel, H.-D. (2006). Qualitätssicherung und -verbesserung von Studium und Lehre durch Evaluation. Akzeptanz und Folgen mehrstufiger Evaluationsverfahren. Beiträge zur Hochschulforschung, 28(2), 6-27.
BORNMANN_L (2006) 68:427 Bornmann, L., Daniel, H.-D. (2006). Selecting scientific excellence through committee peer review - A citation analysis of publications previously published to approval or rejection of post-doctoral research fellowship applicants. Scientometrics, 68(3), 427-440.

## Example WAi network \#(BORNMANN_L) $=61$

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## Temporal

 networksTemporal quantities

Operations
Bibliographic temporal networks

BORNMANN_L DANIEL_H MITTAG_S
$\begin{array}{lll}(2007,2008,1) & (2007,2008,1) \\ (2007,2008,1) & (2007,2008,1) & (2007,2008,1)\end{array}$
$(2007,2008,1) \quad(2007,2008,1)$
$(2006,2007,1) \quad(2006,2007,1)$
(2006, 2007,1)
$(2006,2007,1) \quad(2006,2007,1) \quad(2006,2007,1)$
$(2006,2007,1) \quad(2006,2007,1)$

```
(2006,2007,4), (2007,2008,3)
(2006,2008,3)
(2006,2007,1), (2007, 2008,1)
```

| BORNMANN_L | $(2006,2007,4),(2007,2008,3)$ |
| :--- | :--- |
| DANIEL_H | $(2006,2008,3)$ |
| MITTAG_S | $(2006,2007,1),(2007,2008,1)$ |


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## Multiplication of co-occurence networks

Instantaneous

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A. Ferligoj

Temporal networks

Temporal quantities

Operations
Bibliographic temporal networks

Instantaneous $\mathbf{A}$ on $P \times A$ and $\mathbf{B}$ on $P \times B . \mathbf{C}=\mathbf{A}^{T} . \mathbf{B}$ on $A \times B$.

$$
c_{i j}(t)=\sum_{p \in P} a_{p i}(t)^{T} \cdot b_{p j}(t)
$$

$a_{p i}=\left[\left(d_{p i}, d_{p i}+1, v_{p i}\right)\right]$ and $b_{p j}=\left[\left(d_{p j}, d_{p j}+1, v_{p j}\right)\right]$
for $t=d$ we get

$$
c_{i j}=\left[\left(d, d+1, \sum_{p \in P: d_{p i}=d_{p j}=d} v_{p i} \cdot v_{p j}\right)\right]_{d \in \mathcal{T}}
$$

for $v_{p i}=v_{p j}=1$ we finally get

$$
v_{i j}(d)=\left|\left\{p \in P: d_{p i}=d_{p j}=d\right\}\right|
$$

For binary temporal two-mode networks $\mathbf{A}$ and $\mathbf{B}$ the value $v_{i j}(d)$ of the product $\mathbf{A}^{T}$.B is equal to the number of different members of $P$ with which both $i$ and $j$ have contact in the instant $d$.

## Multiplication of co-occurence networks

Cumulative

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Temporal networks

Temporal quantities Operations

Cumulative $\mathbf{A}$ on $P \times A$ and $\mathbf{B}$ on $P \times B . \mathbf{C}=\mathbf{A}^{T} . \mathbf{B}$ on $A \times B$.

$$
c_{i j}(t)=\sum_{p \in P} a_{p i}(t)^{T} \cdot b_{p j}(t)
$$

$a_{p i}=\left[\left(d_{p i}\right.\right.$, last $\left.\left.+1, v_{p i}\right)\right]$ and $b_{p j}=\left[\left(d_{p j}\right.\right.$, last $\left.\left.+1, v_{p j}\right)\right]$
for $t=d$ we get

$$
c_{i j}=\left[\left(d, d+1, \sum_{p \in P:\left(d_{p i} \leq d\right) \wedge\left(d_{p j} \leq d\right)} v_{p i} \cdot v_{p j}\right)\right]_{d \in \mathcal{T}}
$$

for $v_{p i}=v_{p j}=1$ we finally get

$$
v_{i j}(d)=\left|\left\{p \in P:\left(d_{p i} \leq d\right) \wedge\left(d_{p j} \leq d\right)\right\}\right|
$$

For binary temporal two-mode networks $\mathbf{A}$ and $\mathbf{B}$ the value $v_{i j}(d)$ of the product $\mathbf{A}^{T}$. $\mathbf{B}$ is equal to the number of different members of $P$ with which both $i$ and $j$ have contact in all instants up to including the instant $d$.

## Temporal co-authorship networks

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Temporal networks

Temporal quantities

Using the multiplication of temporal matrices over the combinatorial semiring we get the corresponding instantaneous and cumulative co-occurrence matrices

$$
\mathbf{C i}=\mathbf{A i}^{T} \cdot \mathbf{A} \mathbf{i} \quad \text { and } \quad \mathbf{C} \mathbf{c}=\mathbf{A c}^{T} \cdot \mathbf{A c}
$$

A typical example of such a matrix is the papers authorship matrix WA where $E$ is the set of papers $W, P$ is the set of authors $A$ and $d$ is the publication year.
The triple $(s, f, v)$ in a temporal quantity $c i_{p q}$ tells that in the time interval $[s, f)$ there were $v$ events in which both $p$ and $q$ took part.
The triple ( $s, f, v$ ) in a temporal quantity $c c_{p q}$ tells that in the time interval $[s, f)$ there were in total $v$ accumulated events in which both $p$ and $q$ took part.

The diagonal matrix entries $c i_{p p}$ and $c c_{p p}$ contain the temporal quantities counting the number of events in the time intervals in which the participant $p$ took part.

## Peer review temporal co-authorship networks

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Temporal networks

Temporal quantities

From a collection WoS peer review network we extracted the data about works with complete description: pCiteD, pWAd, pWKd, pWJd, pYearD, pNPd and transformed the network pWAd into corresponding temporal networks pWAdInst pWAdCum in netJSON format.

In the network pWAd we have $|W|=22104,|A|=62106]$, and $n A r c s=80021$.
The matrices

$$
\mathbf{C o i}=\mathbf{W A i}^{T} \cdot \mathbf{W A i} \quad \text { and } \quad \mathbf{C o c}=\mathbf{W} \mathbf{A c}^{T} \cdot \mathbf{W A c}
$$

describe the instantaneous co-autorship temporal network and the cumulative co-autorship temporal network.

Fractional versions of temporal co-authorship networks can be also computed.

## Temporal co-authorship networks

multiply.py

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Temporal networks

Temporal quantities

Operations
Bibliographic temporal networks

Conclusions

```
gdir = 'c:/users/batagelj/work/python/graph/graph'
wdir = 'c:/users/batagelj/work/python/graph/JSON/peere'
cdir = 'c:/users/batagelj/work/python/graph/chart'
import sys, os, datetime, json
sys.path = [gdir]+sys.path; os.chdir(wdir)
import TQ
from GraphNew import Graph
# file = 'C:/Users/batagelj/work/Python/graph/JSON/peere/pWAdCum.json'
file = 'C:/Users/batagelj/work/Python/graph/JSON/peere/pWAdInst.json'
t1 = datetime.datetime.now()
print("started: ",t1.ctime(),"\n")
G = Graph.loadNetJSON(file)
t2 = datetime.datetime.now()
print("\nloaded: ",t2.ctime(),"\ntime used: ", t2-t1)
# T = G.transpose()
# Co = Graph.TQmultiply(T,G,True)
# CR = G.TQtwo2oneRows()
CC = G.TQtwo2oneCols()
t3 = datetime.datetime.now()
print("\ncomputed: ",t3.ctime(),"\ntime used: ", t3-t2)
ia = { v[3]['lab']: k for k,v in CC._nodes.items() }
```


## The most collaborating co-authors

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A. Ferligoj

Temporal networks

Temporal quantities

Operations
Bibliographic temporal networks

Conclusions

```
>>> CC._links[(ia['BORNMANN_L'],ia['DANIEL_H'])][4]['tq']
[(2005, 2006, 4), (2006, 2007, 3), (2007, 2008, 4), (2008, 2009, 7), (2009, 2010, 4),
    (2010, 2011, 11), (2011, 2013, 4), (2015, 2016, 1)]
>>> CC._links[(ia['BROWN_D'],ia['RAFF_H'])][4]['tq']
[(2013, 2014, 11)]
>>> CC._links[(ia['SAPER_C'],ia['MAUNSELL_J'])][4]['tq']
[(2009, 2010, 13), (2010, 2011, 1)]
>>> CC._links[(ia['REYES_H'],ia['ANDRESEN_M'])][4]['tq']
[(1997, 1998, 3), (1998, 1999, 1), (2000, 2002, 1), (2004, 2005, 1), (2005, 2006, 2),
    (2006, 2008, 1), (2009, 2010, 2), (2011, 2012, 1), (2013, 2016, 1)]
>>> CC._links[(ia['KRAVITZ_R'],ia['FELDMAN_M'])][4]['tq']
[(2010, 2016, 1)]
>>> CC._links[(ia['DEANGELI_C'],ia['FONTANAR_P'])][4]['tq']
[(2000, 2002, 1), (2003, 2004, 1), (2005, 2012, 1)]
>>> CC.__links[(ia['DANIEL_H'],ia['DANIEL_H'])][4]['tq']
[(1993, 1994, 3), (2005, 2006, 5), (2006, 2008, 4), (2008, 2009, 7), (2009, 2010, 4),
    (2010, 2011, 11), (2011, 2013, 4), (2014, 2016, 1)]
>>> CC._links[(ia['BORNMANN_L'],ia['BORNMANN_L'])][4]['tq']
    [(2005, 2006, 4), (2006, 2007, 3), (2007, 2008, 4), (2008, 2009, 9), (2009, 2010, 4),
    (2010, 2011, 14), (2011, 2012, 5), (2012, 2013, 7), (2013, 2014, 2), (2014, 2015, 3),
    (2015, 2016, 6)]
>>> bb = CC._links[(ia['BORNMANN_L'],ia['BORNMANN_L'])][4]['tq']
>>> tit = 'BORNMANN_L'
>> TQmax = 15; Tmin = 1995; Tmax = 2016; w = 600; h = 150
>>> Graph.TQshow(bb,cdir,TQmax,Tmin,Tmax,w,h,tit,fill='orange')
```


## PEER <br> Co-authors / pictures

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A. Ferligoj

Temporal networks

Temporal quantities

Operations
Bibliographic temporal networks

Conclusions





## Co-authors / cumulative

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V. Batagelj, A. Ferligoj

## Temporal

 networksTemporal quantities

Operations
Bibliographic temporal networks

Conclusions
file = 'C:/Users/batagelj/work/Python/graph/JSON/peere/pWAdCum.json'
>>> rac = CC._links[(ia['REYES_H'],ia['ANDRESEN_M'])][4]['tq']
>>> tit = 'REYES_H \& ANDRESEN_M'
>>> TQmax $=20 ;$ Tmin $=1995 ; \bar{T} \max =2016 ; \mathrm{w}=600 ; \mathrm{h}=200$
>>> Graph.TQshow(rac, cdir,TQmax,Tmin,Tmax,w,h,tit,fill='brown')


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## Authors and keywords

Using the multiplication of temporal matrices over the combinatorial semiring on bibliographic matrices WA and WK we get the corresponding instantaneous and cumulative matrices

$$
\mathbf{A K i}=\mathbf{W} \mathbf{A i}^{T} \cdot \mathbf{W K i} \quad \text { and } \quad \mathbf{A K c}=\mathbf{W} \mathbf{A c}{ }^{T} \cdot \mathbf{W K c}
$$

The triple ( $s, f, v$ ) in a temporal quantity $a^{2} i_{a k}$ tells that in the time interval $[s, f$ ) the author a used the keyword $k v$ times (in $v$ works).
The triple $(s, f, v)$ in a temporal quantity $a k c_{a k}$ tells that in an instant $t$ in the time interval $[s, f)$ the author a used cumulatively (till time $t$ ) the keyword $k v$ times (in $v$ works).

In September 2016 we developed algorithms for determining temporal ordinary and $P_{S}$-cores that allow us to identify evolving groups in temporal networks.

## Temporal citation networks

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A. Ferligoj

Temporal networks

Temporal quantities

Operations

A citation matrix $\mathbf{C i}$ describes the citation relation $p$ cites $q$. Note that $\quad p$ cites $q \Rightarrow d(p) \geq d(q)$.
Then we can construct its instantaneus version Cii:

$$
c i i_{p q}=[(d(p), d(p)+1,1)] \quad \text { iff } \quad c i_{p q}=1
$$

and its cumulative version Cic:

$$
c i c_{p q}=[(d(p), \text { last }+1,1)] \quad \text { iff } \quad c i_{p q}=1
$$

Temporal versions of:
Bibliographic coupling biCo $=\mathbf{C i} \cdot \mathbf{C i}^{T}$.
Co-citation $\mathbf{c o C i}=\mathbf{C i}{ }^{T}$. $\mathbf{C i}$.
Citations between authors $\mathbf{C a}=\mathbf{W A}^{T} . \mathbf{C i} \cdot \mathbf{W A}$.

$$
\mathbf{A C A}=\mathbf{W A i} \mathbf{i}^{T} \cdot \mathbf{C i i} \cdot \mathbf{W A c}
$$

## Conclusions

- temporal networks approach can give additional insight into bibliographic networks;
- we presented only some examples to show that it works. Many options have still to be elaborated;
- temporal networks methods produce large results. Special methods for identifying and presenting (visualizing) interesting parts need to be developed;
- current version of TQ library is based on matrices. This limits the application of the proposed methods to some thousands of nodes (space and time complexity). A much faster version of TQ library based on a graph representation is under development.
$|A|=62106, n E d g e s(C C)=633977,633977 / 1928608671=0.0003287$

