



Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

# Temporal bibliographic analysis

Vladimir Batagelj, Daria Maltseva

IMFM Ljubljana, IAM UP Koper and NRU HSE Moscow

**SDA workshop:**

**Advances in data science for big and complex data**

University Paris-Dauphine, January 10-11, 2019

# Outline

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

- 1 Web of science
- 2 WoS networks
- 3 Cited works
- 4 Temporal networks
- 5 Network multiplication
- 6 Examples
- 7 Bibliography



Vladimir Batagelj: [vladimir.batagelj@fmf.uni-lj.si](mailto:vladimir.batagelj@fmf.uni-lj.si)

Daria Maltseva: [d\\_malceva@mail.ru](mailto:d_malceva@mail.ru)

Current version of slides (January 12, 2019 at 06:07): [slides PDF](#)

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

To the Web of Science (WoS), Clarivate Analytics's multidisciplinary databases of bibliographic information, we put the query

"social network\*"

Additionally, all the articles from the following journals were collected:

Social Networks, Network Science,  
Social Network Analysis and Mining,  
Journal of Complex Networks

Other network-related journals are **not considered** in WoS:

Computational Social Networks, Applied Network Science,  
Online Social Networks and Media, Connections,  
Journal of Social Structure

We limited the search to the Web of Science Core Collection because for other data bases from WoS the CR-fields (containing citation information) can not be exported. The first data set was collected in 2007, second – in June, 2018.



# WoS record

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

PT J  
AU GRANOVET.MS  
TI STRENGTH OF WEAK TIES  
SO AMERICAN JOURNAL OF SOCIOLOGY  
LA English  
DT Article  
C1 JOHNS HOPKINS UNIV, BALTIMORE, MD 21218 USA.  
CR BARNES JA, 1969, SOCIAL NETWORKS URBA  
BECKER MH, 1970, AM SOCIOL REV, V35, P267  
BERSCHEID E, 1969, INTERPERSONAL ATTRAC  
BOISSEVAIN J, 1968, MAN, V3, P542  
BOTT E, 1957, FAMILY SOCIAL NETWOR  
NR 61  
TC 2156  
PU UNIV CHICAGO PRESS  
PI CHICAGO  
PA 5720 S WOODLAWN AVE, CHICAGO, IL 60637  
SN 0002-9602  
J9 AMER J SOCIOl  
JI Am. J. Sociol.  
PY 1973  
VL 78  
IS 6  
BP 1360  
EP 1380  
PG 21  
SC Sociology  
GA P7726  
UT ISI:A1973P772600003  
ER  
SK IP

# Converting WoS data into networks

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

We applied the program WoS2Pajek 1.5 to the collected data.

The following networks were constructed:

- ① the authorship network  $WA$  on works  $\times$  authors (from the field AU),
- ② the journalship network  $WJ$  on works  $\times$  journals (from the field CR or J9),
- ③ the keywordship network  $WK$  on works  $\times$  keywords (from the field ID or DE or TI),
- ④ the citation network  $Cite$  on works (from the field CR).

We obtained also the following node properties:

- ① the partition  $year$  of works by publication year,
- ② the  $DC$  partition distinguishing between works with complete description ( $DC=1$ ) and the cited only works ( $DC=0$ ),
- ③ the vector of number of pages  $NP$ .

We call a *terminal* node a node without a description in the collected data set – it appears only in the WoS CR field as a reference.

We additionally collected on WoS and Google data for terminal nodes with large indegree in the citation network – highly cited works without description in the collected data set.

If a description of a node was not available in WoS we **manually** constructed a corresponding description **without** CR data (using RIS bibliographic format and converting it to WoS).

As the data set of 2007 was already completed, we made this additional search only for works 2008-\* in July 2018.

# Sizes of Original cleaned and Reduced networks

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

|              | # nodes (sum)  | # nodes 1     | # nodes 2     | # arcs    |
|--------------|----------------|---------------|---------------|-----------|
| CiteN        | 1,297,133      |               |               | 2,753,633 |
| <b>CiteR</b> | <b>70,792</b>  |               |               | 398,199   |
| WAn          | 1,693,104      | 1,297,133     | 395,971       | 1,442,240 |
| <b>WAr</b>   | <b>163,803</b> | <b>70,792</b> | <b>93,011</b> | 215,901   |
| WKn          | 1,329,542      | 1,297,133     | 32,409        | 1,167,670 |
| <b>WKr</b>   | <b>103,201</b> | <b>70,792</b> | <b>32,409</b> | 1,167,666 |
| WJn          | 1,366,279      | 1,297,133     | 69,146        | 720,044   |
| <b>WJr</b>   | <b>79,735</b>  | <b>70,792</b> | <b>8,943</b>  | 61,741    |

An important property of all these networks is that they share as the first node set the same set of works (papers, reports, books, etc.) – they are *linked*.

# Cite net

## The most cited works - indegree

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

| i  | freq | id                             | i  | freq | id                              |
|----|------|--------------------------------|----|------|---------------------------------|
| 1  | 5348 | <b>WASSERMAN_S(1994):</b>      | 31 | 734  | *NEWMAN_M(2001)98:404           |
| 2  | 4471 | <b>GRANOVET_M(1973)78:1360</b> | 32 | 719  | *NEWMAN_M(2010):                |
| 3  | 2906 | *WATTS_D(1998)393:440          | 33 | 701  | PORTES_A(1998)24:1              |
| 4  | 2614 | *BARABASI_A(1999)286:509       | 34 | 687  | BLEI_D(2003)3:993               |
| 5  | 2561 | <b>FREEMAN_L(1979)1:215</b>    | 35 | 670  | <b>BURT_R(2004)110:349</b>      |
| 6  | 2447 | BOYD_D(2007)13:210             | 36 | 654  | HANSEN_M(1999)44:82             |
| 7  | 2429 | MCPHERSON_M(2001)27:415        | 37 | 639  | PALLA_G(2005)435:814            |
| 8  | 2330 | <b>BURT_R(1992):</b>           | 38 | 634  | *CLAUSET_A(2004)70:066111       |
| 9  | 1886 | <b>COLEMAN_J(1988)94:95</b>    | 39 | 629  | *BONACICH_P(1987)92:1170        |
| 10 | 1572 | *NEWMAN_M(2003)45:167          | 40 | 628  | ERDOS_P(1959)6:290              |
| 11 | 1520 | *GIRVAN_M(2002)99:7821         | 41 | 628  | UZZI_B(1997)42:35               |
| 12 | 1510 | <b>PUTNAM_R(2000):</b>         | 42 | 628  | <b>ROGERS_E(2003):</b>          |
| 13 | 1285 | *ALBERT_R(2002)74:47           | 43 | 613  | <b>PUTNAM_R(1993):</b>          |
| 14 | 1240 | <b>GRANOVET_M(1985)91:481</b>  | 44 | 593  | BERKMAN_L(1979)109:186          |
| 15 | 1192 | SCOTT_J(2000):                 | 45 | 583  | ZACHARY_W(1977)33:452           |
| 16 | 1171 | <b>EVERETT_M(2002):</b>        | 46 | 572  | <b>BORGATTI_S(2009)323:892</b>  |
| 17 | 1166 | NEWMAN_M(2004)69:026113        | 47 | 569  | *NEWMAN_M(2001)64:025102        |
| 18 | 1093 | <b>COLEMAN_J(1990):</b>        | 48 | 565  | <b>BURT_R(2005):</b>            |
| 19 | 1058 | STEINFELD_C(2007)12:1143       | 49 | 561  | ADLER_P(2002)27:17              |
| 20 | 1034 | FORTUNATO_S(2010)486:75        | 50 | 559  | <b>CHRISTAK_N(2008)358:2249</b> |
| 21 | 999  | <b>BORGATTI_S(2002):</b>       | 51 | 555  | <b>ROGERS_E(1995):</b>          |
| 22 | 945  | <b>CHRISTAK_N(2007)357:370</b> | 52 | 554  | MILGRAM_S(1967)1:61             |
| 23 | 867  | <b>FREEMAN_L(1977)40:35</b>    | 53 | 553  | BARON_R(1986)51:1173            |
| 24 | 854  | HANNEMAN_R(2005):              | 54 | 550  | <b>GRANOVET_M(1978)83:1420</b>  |
| 25 | 800  | <b>LIN_N(2001):</b>            | 55 | 539  | <b>FISCHER_C(1982):</b>         |
| 26 | 757  | KAPLAN_A(2010)53:59            | 56 | 537  | BRIN_S(1998)30:107              |
| 27 | 756  | *BLONDEL_V(2008):P10008        | 57 | 524  | <b>MARSDEN_P(1990)16:435</b>    |
| 28 | 742  | NAHAPIET_J(1998)23:242         | 58 | 523  | KEMP_D(2003):137                |
| 29 | 740  | FORNELL_C(1981)18:39           | 59 | 523  | KLEINBERG_J(1999)46:604         |
| 30 | 740  | *NEWMAN_M(2006)103:8577        | 60 | 517  | *BOCCALET_S(2006)424:175        |

Labels ending with : represent books



# Temporal networks

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

A *temporal network*  $\mathcal{N}_T = (\mathcal{V}, \mathcal{L}, \mathcal{T}, \mathcal{P}, \mathcal{W})$  is obtained by attaching the *time*,  $\mathcal{T}$ , to an ordinary network where  $\mathcal{T}$  is a set of *time points*,  $t \in \mathcal{T}$ .

In a temporal network, nodes  $v \in \mathcal{V}$  and links  $l \in \mathcal{L}$  are not necessarily present or active in all time points. Let  $T(v)$ ,  $T \in \mathcal{P}$ , be the *activity set* of time points for node  $v$  and  $T(l)$ ,  $T \in \mathcal{W}$ , the activity set of time points for link  $l$ .

Besides the presence/absence of nodes and links also their properties can change through time.

# Temporal quantities

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

We introduce a notion of a *temporal quantity*

$$a(t) = \begin{cases} a'(t) & t \in T_a \\ \text{\texttt{X}} & t \in \mathcal{T} \setminus T_a \end{cases}$$

where  $T_a$  is the *activity time set* of  $a$  and  $a'(t)$  is the value of  $a$  in an instant  $t \in T_a$ , and  $\text{\texttt{X}}$  denotes the value *undefined*.

We assume that the values of temporal quantities belong to a set  $A$  which is a *semiring*  $(A, +, \cdot, 0, 1)$  for binary operations  $+$  and  $\cdot$ .

We can extend both operations to the set  $A_{\text{\texttt{X}}} = A \cup \{\text{\texttt{X}}\}$  by requiring that for all  $a \in A_{\text{\texttt{X}}}$  it holds

$$a + \text{\texttt{X}} = \text{\texttt{X}} + a = a \quad \text{and} \quad a \cdot \text{\texttt{X}} = \text{\texttt{X}} \cdot a = \text{\texttt{X}}.$$

The structure  $(A_{\text{\texttt{X}}}, +, \cdot, \text{\texttt{X}}, 1)$  is also a semiring.

# Operations with temporal quantities

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

Let  $A_{\mathbb{M}}(\mathcal{T})$  denote the set of all temporal quantities over  $A_{\mathbb{M}}$  in time  $\mathcal{T}$ . To extend the operations to networks and their matrices we first define the *sum* (parallel links)  $a + b$  as

$$(a + b)(t) = a(t) + b(t) \quad \text{and} \quad T_{a+b} = T_a \cup T_b.$$

The *product* (sequential links)  $a \cdot b$  is defined as

$$(a \cdot b)(t) = a(t) \cdot b(t) \quad \text{and} \quad T_{a \cdot b} = T_a \cap T_b.$$

Let us define the temporal quantities **0** and **1** with requirements  $\mathbf{0}(t) = \emptyset$  and  $\mathbf{1}(t) = 1$  for all  $t \in \mathcal{T}$ . Again, the structure  $(A_{\mathbb{M}}(\mathcal{T}), +, \cdot, \mathbf{0}, \mathbf{1})$  is a semiring.

# Addition of temporal quantities

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

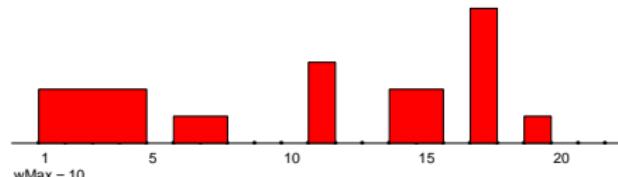
Temporal  
networks

Network  
multiplication

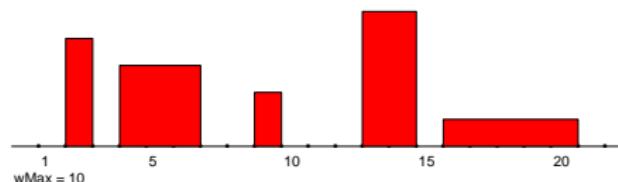
Examples

Bibliography

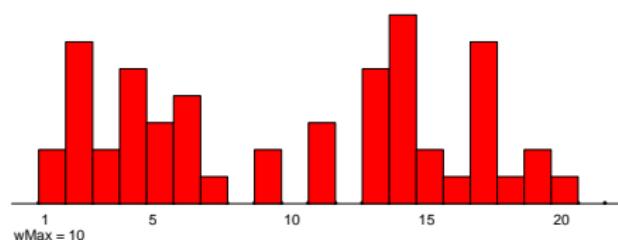
$a :$



$b :$



$a + b :$



# Multiplication of temporal quantities

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

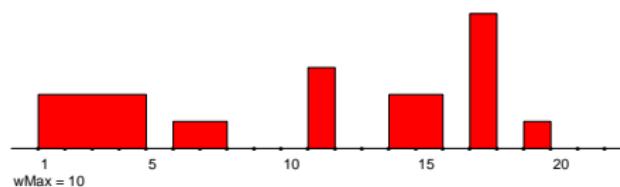
Temporal  
networks

Network  
multiplication

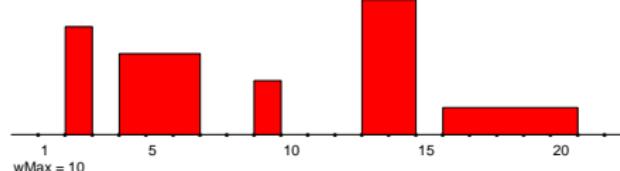
Examples

Bibliography

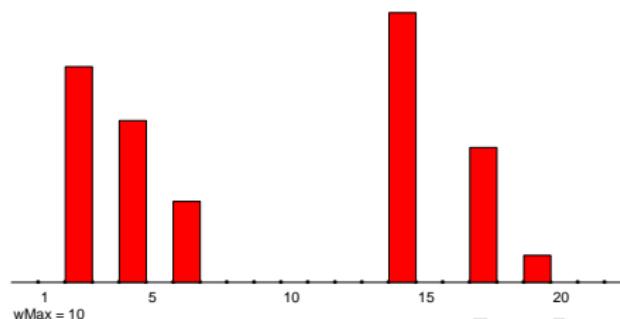
$a :$



$b :$



$a \cdot b :$



# Creating temporal networks

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

Let the binary matrix  $\mathbf{A} = [a_{ep}]$  describe a two-mode (or one-mode) network on the set of events  $E$  and the set of participants  $P$ :

$$a_{ep} = \begin{cases} 1 & p \text{ participated in the event } e \\ 0 & \text{otherwise} \end{cases}$$

The function  $d : E \rightarrow \mathcal{T}$  assigns to each event  $e$  the date  $d(e)$  when it happened.  $\mathcal{T} = [\text{first}, \text{last}] \subset \mathbb{N}$ . Using these data we can construct two temporal affiliation matrices:

- **instantaneous  $\mathbf{Ai} = [ai_{ep}]$** , where

$$ai_{ep} = \begin{cases} [(d(e), d(e) + 1, 1)] & a_{ep} = 1 \\ [] & \text{otherwise} \end{cases}$$

- **cumulative  $\mathbf{Ac} = [ac_{ep}]$** , where

$$ac_{ep} = \begin{cases} [(d(e), last + 1, 1)] & a_{ep} = 1 \\ [] & \text{otherwise} \end{cases}$$

# Temporal networks in Nets

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

```
>>> net = wdir+"/WAins.json"
>>> WAi = N.loadNetJSON(net)
>>> I = WAi.Index()
>>> I["ERDOS_P(1959)6:290"]
776
>>> WAi._nodes[776]
[{}, {}, {71246: [1091], 89670: [214562]},
{'mode': 1, 'lab': 'ERDOS_P(1959)6:290', 'act': [[1959, 2019, 1]]}]
>>> WAi._nodes[71246]
[{}, {776: [1091], 11539: [25213], 11540: [25214], 15565: [33820],
42898: [129167]}, {}, {'mode': 2, 'lab': 'ERDOS_P', 'act': [[1894, 2019, 1]]}]
>>> WAi._nodes[89670]
[{}, {776: [214562], 15565: [215596]}, {}, {'mode': 2, 'lab': 'RENYI_A', 'act': [[1894, 2019, 1]]}]
>>> WAi._links[1091]
[776, 71246, True, None, {'tq': [[1959, 1960, 1]]}]
>>> WAi._links[214562]
[776, 89670, True, None, {'tq': [[1959, 1960, 1]]}]
```

# Temporal citation networks

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

```
gdir = 'C:/Users/batagelj/work/Python/graph/Nets'
wdir = "C:/Users/batagelj/work/Python/WoS/SocNet/2018/Time/cite"
cdir = "C:/Users/batagelj/work/Python/WoS/SocNet/2018/Time/work/chart"
import sys, os, re, datetime, json
sys.path = [gdir]+sys.path; os.chdir(wdir)
from TQ import *
from Nets import Network as N
Ci = N.loadNetJSON(wdir+"/CiteIns.json")
Cu = N.loadNetJSON(wdir+"/CiteCum.json")
L = [ "#WASSERMA_S(1994):", "#GRANOVET_M(1973)78:1360", "WATTS_D(1998)393:440",
      "BARABASI_A(1999)286:509", "FREEMAN_L(1979)1:215", "#BOYD_D(2007)13:210",
      "MCPHERSO_M(2001)27:415", "BURT_R(1992):" ]
I = Ci.Index()
-----
>>> I["#WASSERMA_S(1994):"]
33
>>> TCin = [ (u, Ci.TQnetInDeg(I[u])) for u in L ]
>>> TCuin = [ (u, Cu.TQnetInDeg(I[u])) for u in L ]
>>> TCin[0]
('#WASSERMA_S(1994):', [(1994, 1995, 2), (1995, 1996, 7), (1996, 1997, 12), (1997, 1998, 23),
(1998, 1999, 26), (1999, 2000, 41), (2000, 2001, 31), (2001, 2002, 54), (2002, 2003, 38),
(2003, 2004, 64), (2004, 2005, 76), (2005, 2006, 85), (2006, 2007, 103), (2007, 2008, 220),
(2008, 2009, 238), (2009, 2010, 313), (2010, 2011, 364), (2011, 2012, 424), (2012, 2013, 459),
(2013, 2014, 438), (2014, 2015, 504), (2015, 2016, 579), (2016, 2017, 552), (2017, 2018, 528),
(2018, 2019, 167)])
>>> TCuin[0]
('#WASSERMA_S(1994):', [(1994, 1995, 2), (1995, 1996, 9), (1996, 1997, 21), (1997, 1998, 44),
(1998, 1999, 70), (1999, 2000, 111), (2000, 2001, 142), (2001, 2002, 196), (2002, 2003, 234),
(2003, 2004, 298), (2004, 2005, 374), (2005, 2006, 459), (2006, 2007, 562), (2007, 2008, 782),
(2008, 2009, 1020), (2009, 2010, 1333), (2010, 2011, 1697), (2011, 2012, 2121),
(2012, 2013, 2580), (2013, 2014, 3018), (2014, 2015, 3522), (2015, 2016, 4101),
(2016, 2017, 4653), (2017, 2018, 5181), (2018, 2019, 5348)])
>>> w = 800; h = 500
>>> p=0; (Tmin,Tmax,tt,TQmax) = TQ.TqSummary(TCin[p][1]); tit = TCin[p][0]
>>> N.TQshow(TCin[p][1],cdir,TQmax,Tmin,Tmax,w,h,tit,fill='red')
```

# Temporal citation network

## temporal indegrees

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

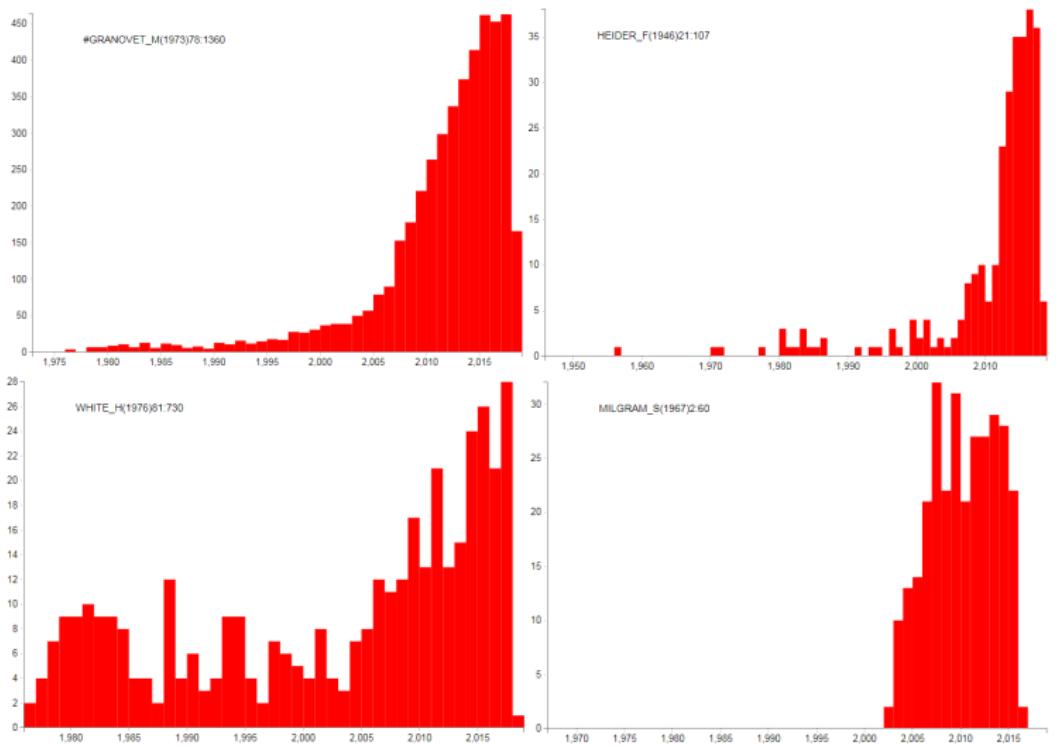
Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography



# Authors Collaboration

## Network Co

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

$$\mathbf{Co} = \mathbf{WA}^T * \mathbf{WA}$$

The weight of the edges between the nodes  $i$  and  $j$  is equal to total number of works author  $i$  and  $j$  wrote together.

The values of loops in **Co** are equal to the total number of works that each author have (which is also equal to the indegree values of the **WA** network).

The proposed approach has some *limitations*, such as the overrating of the contribution of works with many authors. To make the contribution of each work equal we have to use the normalized version  $n(\mathbf{WA})$  of the network (matrix) (*fractional approach*)

$$n(\mathbf{WA})[w, a] = \frac{\mathbf{WA}[w, a]}{\max(1, \text{outdeg}[w])}$$

# Multiplication of networks

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

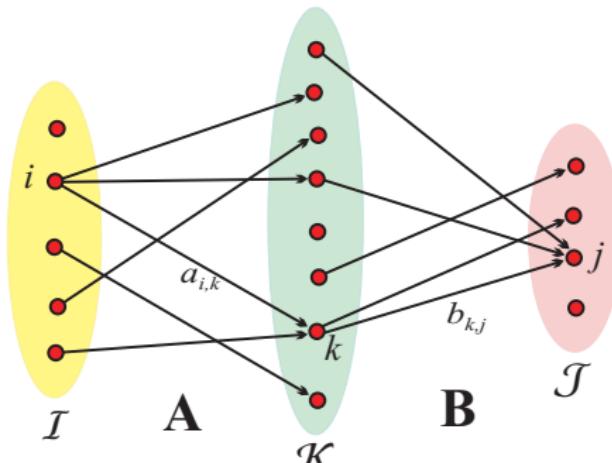
Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography



$$c_{i,j} = \sum_{k \in N_A(i) \cap N_B^-(j)} a_{i,k} \cdot b_{k,j}$$

If all weights in networks  $\mathcal{N}_A$  and  $\mathcal{N}_B$  are equal to 1 the value of  $c_{i,j}$  counts the number of ways we can go from  $i \in \mathcal{I}$  to  $j \in \mathcal{J}$  passing through  $\mathcal{K}$ .

# Derived networks

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

$$\mathbf{AK} = \mathbf{WA}^T * \mathbf{WK}$$

The weight of the arc from the node  $a$  to the node  $k$  is equal to the number of works in which the author  $a$  used the keyword  $k$ .

$$\mathbf{CiteJ} = (\mathbf{WJ})^T * \mathbf{Cite} * \mathbf{WJ}$$

the value of weight of the element  $[u,v]$  is equal to the **number of citations** from journal  $i$  to journal  $j$ .

$$\mathbf{CiteAn} = (\mathbf{WA})^T * n(\mathbf{Cite}) * \mathbf{WA}$$

The value of element  $\text{CiteAn}[u,v]$  is equal to the number of **fractional contribution** of citations from works coauthored by  $u$  to works coauthored by  $v$ .

etc.

# Multiplication of co-occurrence networks

## Instantaneous

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

Instantaneous **A** on  $P \times A$  and **B** on  $P \times B$ .  $\mathbf{C} = \mathbf{A}^T \cdot \mathbf{B}$  on  $A \times B$ .

$$c_{ij}(t) = \sum_{p \in P} a_{pi}(t)^T \cdot b_{pj}(t)$$

$a_{pi} = [(d_{pi}, d_{pi} + 1, v_{pi})]$  and  $b_{pj} = [(d_{pj}, d_{pj} + 1, v_{pj})]$   
for  $t = d$  we get

$$c_{ij} = [(d, d + 1, \sum_{p \in P: d_{pi}=d_{pj}=d} v_{pi} \cdot v_{pj})]_{d \in \mathcal{T}}$$

for  $v_{pi} = v_{pj} = 1$  we finally get

$$v_{ij}(d) = |\{p \in P : d_{pi} = d_{pj} = d\}|$$

For binary temporal two-mode networks **A** and **B** the value  $v_{ij}(d)$  of the product  $\mathbf{A}^T \cdot \mathbf{B}$  is equal to the number of different members of  $P$  with which both  $i$  and  $j$  have contact in the instant  $d$ .

# Multiplication of co-occurrence networks

## Cumulative

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

Cumulative **A** on  $P \times A$  and **B** on  $P \times B$ .  $\mathbf{C} = \mathbf{A}^T \cdot \mathbf{B}$  on  $A \times B$ .

$$c_{ij}(t) = \sum_{p \in P} a_{pi}(t)^T \cdot b_{pj}(t)$$

$a_{pi} = [(d_{pi}, \text{last} + 1, v_{pi})]$  and  $b_{pj} = [(d_{pj}, \text{last} + 1, v_{pj})]$   
for  $t = d$  we get

$$c_{ij} = [(d, d + 1, \sum_{p \in P: (d_{pi} \leq d) \wedge (d_{pj} \leq d)} v_{pi} \cdot v_{pj})]_{d \in \mathcal{T}}$$

for  $v_{pi} = v_{pj} = 1$  we finally get

$$v_{ij}(d) = |\{p \in P : (d_{pi} \leq d) \wedge (d_{pj} \leq d)\}|$$

For binary temporal two-mode networks **A** and **B** the value  $v_{ij}(d)$  of the product  $\mathbf{A}^T \cdot \mathbf{B}$  is equal to the number of different members of  $P$  with which both  $i$  and  $j$  have contact in all instants up to including the instant  $d$ .

# Citations among journals

JCJ and JCJn from WJins, WJcum, CiteIns nets

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

$$\mathbf{JCJ} = (\mathbf{WJins})^T * \mathbf{CiteIns} * \mathbf{WJcum}$$

The value of weight of the element  $JCJ[i,j]$  is equal to the **number of citations** per year from journal  $i$  to journal  $j$ .

$$\mathbf{JCJn} = (\mathbf{WJins})^T * n(\mathbf{CiteIns}) * \mathbf{WJcum}$$

where

$$n(\mathbf{CiteIns})[u, v] = \frac{\mathbf{CiteIns}[u, v]}{\max(1, \text{outdeg}(u))}$$

The value of element  $JCJn[i,j]$  is equal to the number of **fractional contribution** of citations per year from journal  $i$  to journal  $j$ .

# Self-citations of journals

## Loops from JCJ network

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

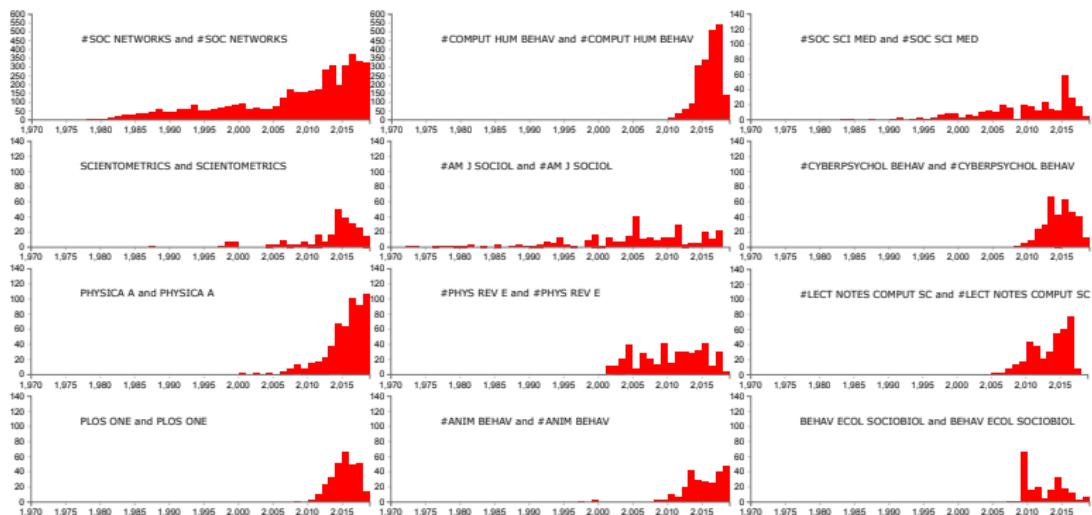
Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography



# Citations of Social Networks journal InSum and OutSum of JCJ network without loops

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

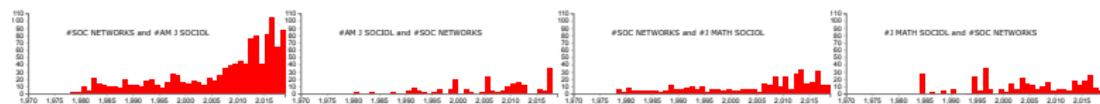
Temporal  
networks

Network  
multiplication

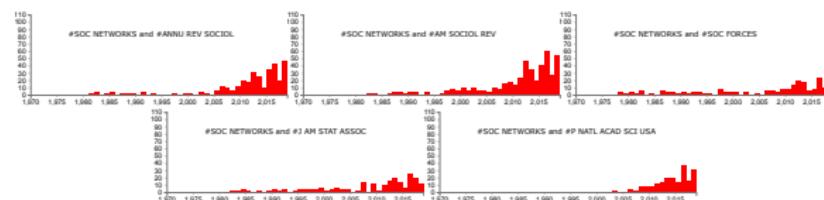
Examples

Bibliography

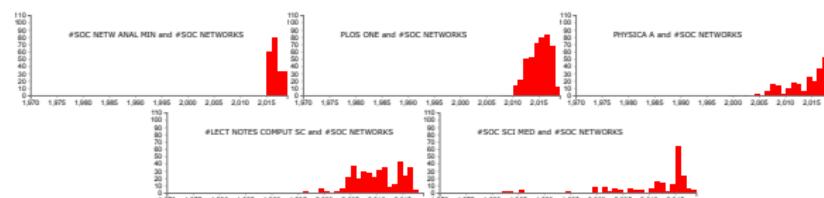
## OutSum and InSum:



## OutSum:



## InSum:



# Citation of general scientific journals from JCJ network without loops

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

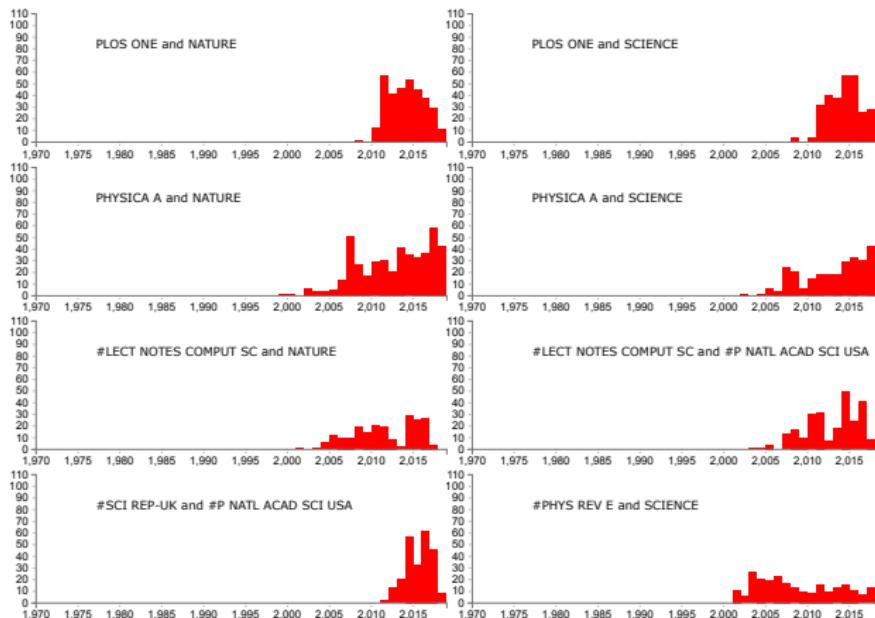
Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography



# Citations of other journals from JCJ network without loops

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

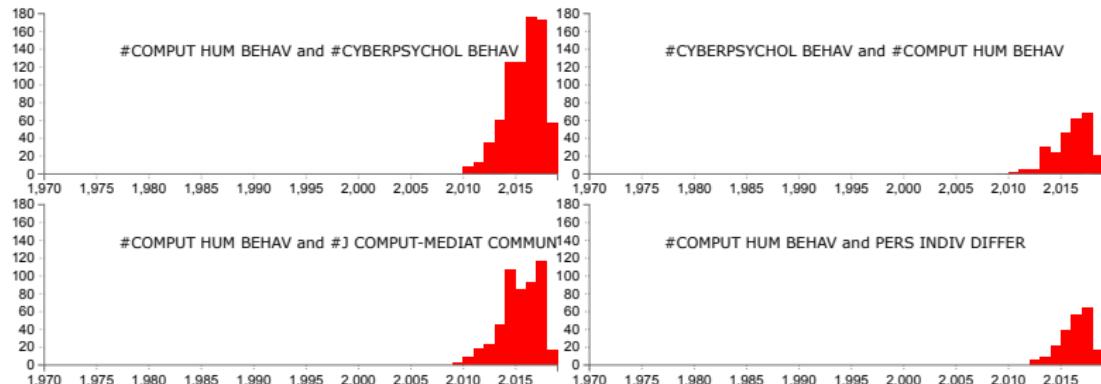
Temporal  
networks

Network  
multiplication

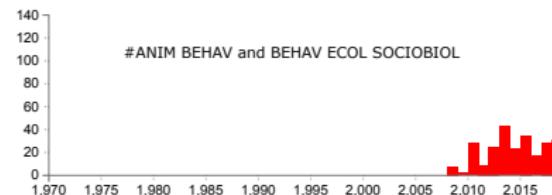
Examples

Bibliography

## Computer Science:



## Animal social networks:



# Outgoing citations with/without loops from JCJn network

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

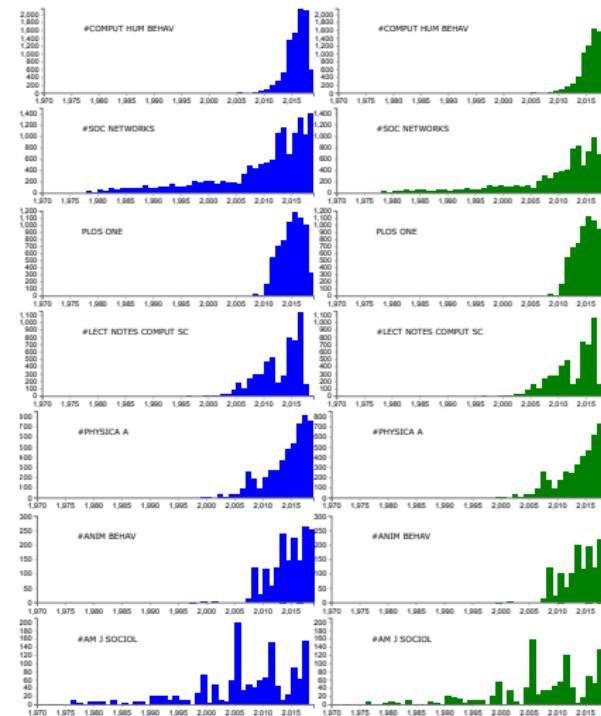
Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography



# Incoming citations with/without loops from JCJn network

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

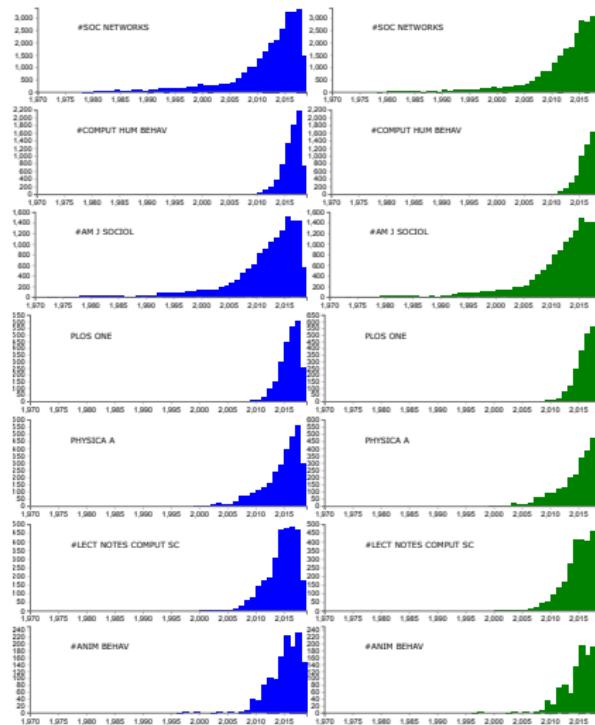
Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography



# Bibliography I

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

- ① Batagelj, V. (2007) WoS2Pajek. Networks from Web of Science. Version 0.3. Manual. URL: <http://vlado.fmf.uni-lj.si/pub/networks/pajek/WoS2Pajek/WoS2Pajek.pdf>
- ② Batagelj V., Cerinšek M. (2013). On bibliographic networks. *Scientometrics*. 96 (3), 845-864
- ③ Batagelj, V., Doreian P., V., Ferligoj, A., Kejzar N. Understanding Large Temporal Networks and Spatial Networks: Exploration, Pattern Searching, Visualization and Network Evolution, 2014.
- ④ Batagelj, V., Ferligoj, A. Squazzoni, F. The emergence of a field: a network analysis of research on peer review. *Scientometrics* (2017) 113: 503. <https://doi.org/10.1007/s11192-017-2522-8>
- ⑤ Batagelj, V, Cerinšek, M (2013). On bibliographic networks. *Scientometrics* 96(3), 845-864.

# Bibliography II

Temporal  
bibliographic  
analysis

V. Batagelj,  
D. Maltseva

Web of  
science

WoS networks

Cited works

Temporal  
networks

Network  
multiplication

Examples

Bibliography

- 6 Batagelj, V, Doreian, P, Ferligoj, A, Kejžar, N (2014). *Understanding Large Temporal Networks and Spatial Networks: Exploration, Pattern Searching, Visualization and Network Evolution*. Wiley.
- 7 Batagelj, V, Praprotnik, S (2016): An algebraic approach to temporal network analysis based on temporal quantities. *Social Network Analysis and Mining*, 6(1), 1-22.
- 8 Batagelj, V (2017): **Nets** – a Python package for network analysis. <https://github.com/bavla/Nets>
- 9 Batagelj, V (2018): Python Packages for Networks. In: Alhajj R., Rokne J. (eds) *Encyclopedia of Social Network Analysis and Mining*. Springer, New York, NY