

### Latest developments of the RSDA 2.0: An R package for Symbolic Data Analysis

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## To install the package from CRAN

✓ install.packages("RSDA",dependencies=TRUE)

# To load the package✓ library(RSDA)

### To get help about the package ✓ ?RSDA

RSDA {RSDA}



**R** Documentation

### R to Symbolic Data Analysis

#### Description

This work is framed inside the Symbolic Data Analysis (SDA). The objective of this work is to implement in R to the symbolic case certain techniques of the automatic classification, as well as some lineal models. These implementations will always be made following two fundamental principles in Symbolic Data Analysis like they are: Classic Data Analysis should always be a case particular case of the Symbolic Data Analysis and both, the exit as the input in an Symbolic Data Analysis should be symbolic. We implement for variables of type interval the mean, the median, the mean of the extreme values, the standard deviation, the deviation quartil, the dispersion boxes and the correlation also three new methods are also presented to carry out the lineal regression for variables of type interval. We also implement in this R package the method of Principal Components Analysis in two senses: First, we propose three ways to project the interval variables in the circle of correlations in such way that is reflected the variation or the inexactness of the variables. Second, we propose an algorithm to make the Principal Components Analysis for variables of type histogram. We implement a method for multidimensional scaling of interval data, denominated INTERSCAL.

#### Details

Package: RSDA Type: Package Version: 2.0 Date: 2015-10-01 License: GPL (>=2)

Most of the function of the package stars from a symbolic data table that can be store in a CSV file withe follwing forma: In the first row the labels \$C means that follows a continuous variable, \$I means an interval variable, \$H means a histogram variables and \$S means set variable. In the first row each labels should be follow of a name to variable and to the case of histogram a set variables types the names of the modalities (categories). In data rows for continuous variables we have just one value, for interval variables we have the minimum and the maximum of the interval, for histogram variables we have the number of modalities and then the probability of each modality and for set variables we have the cardinality of the set and next the elements of the set.

#### Author(s)

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#### References

Billard L. and Diday E. (2006). Symbolic data analysis: Conceptual statistics and data mining. Wiley, Chichester.

Billard L., Douzal-Chouakria A. and Diday E. (2011) Symbolic Principal Components For Interval-Valued Observations, Statistical Analysis and Data Mining. 4 (2), 229-246. Wiley.

# What is new in RSDA 2.0?



- Symbolic Data Frame
- New distances between symbolic objects
- Radar (star) plots for interval variables
- Histogram distribution for interval variables
- New PCA methods (optimized, tops, principals curves)
- Now RSDA is in GitHub to collaborate to RSDA



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Millions ...

		Id-trx	Trans Type	Com	nerce Loc	Amount	Card Num		
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	Cases	3245	35						
		5367	27			1,900.00	1002		
		6486	34			1,600.00	1002		
Hundreds									
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S	ymbolic Data	1000	36(1/2),3	<b>89(1/2)</b>	{ <i>Curr-50%</i>	,Gre-50%}	[2.4,2.5]	255.4	
	Table	1001	28(1/3),3	85(2/3)	{ <b>SP-66%</b> ,A	l <b>l-33%</b> }	[1.75,1.9]	122,2	
	Concepts	1002	27(1/2),3	84(1/2)	{Al-50%,H	er-50%}	[1.6,1.9]	534,5	
	Concepto								



	Classical d	Schools		
Schools	Town	Nb of pupils	Kind	Level
Jaurès	Paris	320	Public	1
Condorcet	Paris	450	Public	3
Chevreul	Lyon	200	Public	2
St Hélène	Lyon	380	Private	3
St Sernin	Toulouse	290	Public	1
St Hilaire	Toulouse	210	Private	2

### Symbolic description of the towns by the schools variables

Town	Nb of pupils	Kind	Level
Paris	[320, 450]	(100%)Public	{1, 3}
Lyon	[200, 380]	(50%)Public, (50%)Private	{2, 3}
Toulouse	[210, 290]	(50%)Public, (50%)Private	{1, 2}

Sec. and	

i	Name	Month	Food	Social	Travel	Gas	Clothes
1	Jon	February	23.65	14.56	218.02	16.79	45.61
2	Leigh	May	28.47	8.99	141.60	21.74	86.04
3	Leigh	July	30.86	9.55	193.14	24.26	95.68
4	Tom	July	24.13	15.97	190.40	35.71	20.02
5	Jon	April	23.40	11.61	179.38	23.73	48.89
6	Jon	November	23.11	16.71	178.78	20.55	47.96
7	Leigh	September	32.14	12.34	165.65	17.62	66.40
8	Leigh	August	25.92	20.78	201.18	32.97	70.96
9	Leigh	November	31.52	16.62	177.50	20.95	71.18
10	Jon	November	23.11	14.41	179.86	20.53	51.49

Table 2.3 Credit card dataset.

Table 2.4 Credit card use by person-months.

Name – Month	Food	Social	Travel	Gas	Clothes
Jon – January	[20.81, 29.38]	[9.74, 18.86]	[192.33, 205.23]	[13.01, 24.42]	[44.28, 53.82]
Jon – February	[21.44, 27.58]	[10.86, 18.01]	[214.98, 229.63]	[16.08, 22.86]	[50.51, 63.57]
: :				:	:
Tom – January	[23.28, 30.00]	[8.67, 18.31]	[193.53, 206.53]	[26.28, 35.61]	[15.51, 25.66]
Tom – February	[20.61, 28.66]	[10.66, 17.20]	[195.53, 203.83]	[25.43, 34.18]	[12.99, 24.88]
: :	÷	÷	:	÷	÷
Leigh – January	[25.59, 35.33]	[7.07, 19.00]	[194.12, 207.05]	[17.75, 23.07]	[61.47, 75.43]
Leigh – February	[31.30, 40.80]	[9.05, 24.44]	[212.76, 227.43]	[13.81, 25.08]	[71.63, 85.58]
: :	:	:	÷	:	:

## Center and Range Method (CRM)

Then the <u>center</u> least square estimate of β is computed by:

$$\hat{\boldsymbol{\beta}}^{c} = ((\mathbf{X}^{c})^{T}\mathbf{X}^{c})^{-1}(\mathbf{X}^{c})^{T}\mathbf{y}^{c}$$

Then the <u>range</u> least square estimate of β is computed by:

$$\hat{\boldsymbol{\beta}}^{r} = ((\mathbf{X}^{r})^{T}\mathbf{X}^{r})^{-1}(\mathbf{X}^{r})^{T}\mathbf{y}^{r}$$

> The response value is fitted as follows:  $\hat{y} = [\hat{y}_L, \hat{y}_U]$  $\hat{y}_L = \hat{y}^c - \hat{y}^r$  and  $\hat{y}_U = \hat{y}^c + \hat{y}^r$ , where,  $\hat{y}^c = (\tilde{\mathbf{x}}^c)^T \hat{\boldsymbol{\beta}}^c$ ,  $\hat{y}^r = (\tilde{\mathbf{x}}^r)^T \hat{\boldsymbol{\beta}}^r$ 

## **Ridge** Center and Range Method



For the *center* least square estimate of β is computed by:

$$\hat{eta}^{c^{\mathbf{ridge}}} = \left( \left( \mathbf{X}^{c} 
ight)^{T} \left( \mathbf{X}^{c} 
ight) + \lambda \mathbf{I} 
ight)^{-1} \left( \mathbf{X}^{c} 
ight)^{T} \mathbf{y}^{c}$$

Then the <u>range</u> least square estimate of β is computed by:

$$\hat{\beta}^{r^{\mathrm{ridge}}} = \left( \left( \mathbf{X}^{r} \right)^{T} \left( \mathbf{X}^{r} \right) + \lambda \mathbf{I} \right)^{-1} \left( \mathbf{X}^{r} \right)^{T} \mathbf{y}^{r}$$

> The response value is fitted as follows:  $\hat{y} = [\hat{y}_L, \hat{y}_U]$  $\hat{y}_L = \hat{y}^c - \hat{y}^r$  and  $\hat{y}_U = \hat{y}^c + \hat{y}^r$ , where  $\hat{y}^c = (\tilde{x}^c)^T \hat{\beta}^{c^{ridge}}$  and  $\hat{y}^r = (\tilde{x}^c) \hat{\beta}^{r^{ridge}}$ 

## Lasso Center and Range Method



Then the <u>center</u> least square estimate of β is obtained solving the following optimization problem:

$$\hat{\beta}^{c^{\text{lasso}}} = \operatorname{argmin}_{\beta} \left\{ \sum_{i=1}^{N} (y_i^c - \beta_0 - \sum_{j=1}^{p} x_{ij}^c \beta_j)^2 + \lambda \sum_{j=1}^{p} |\beta_j| \right\}$$

Then the <u>range</u> least square estimate of β is obtained solving the following optimization problem:

$$\hat{\beta}^{r^{\text{lasso}}} = \underset{\beta}{\operatorname{argmin}} \left\{ \sum_{i=1}^{n} \left( \left( y_{i}^{r} - \beta_{0} - \sum_{\substack{j=1\\ \hat{\beta}_{j}^{c^{\text{lasso}}} \neq 0}}^{p} x_{ij}^{r} \beta_{j} \right)^{2} + \lambda \sum_{\substack{j=1\\ \hat{\beta}_{j}^{c^{\text{lasso}}} \neq 0}}^{p} |\beta_{j}| \right\}$$

## Lasso Center and Range Method



> Then the response value is fitted as follows:  $\hat{y} = [\hat{y_L}, \hat{y_U}]$ 

$$\begin{vmatrix} \hat{y}_L = \hat{y}^c - \hat{y}^r \end{vmatrix}$$
 and  $\begin{vmatrix} \hat{y}_U = \hat{y}^c + \hat{y}^r \end{vmatrix}$   
where  $\hat{y}^c = (\tilde{x}^c)^T \hat{\beta}^{c^{\text{lasso}}}$  and  $\hat{y}^r = (\tilde{x}^c) \hat{\beta}^{r^{\text{lasso}}}$ 

➤ The optimal value of λ is computed using Cross-Validation:



## **Elastic Net** Center Method (ECM)

> The center least square estimate of  $\beta$  is obtained solving the following optimization problem:

$$\hat{\beta}^{\text{NET}} = \operatorname{argmin}_{\beta} \left\{ \sum_{i=1}^{N} (y_i^c - \beta_0 - \sum_{j=1}^{p} x_{ij}^c \beta_j)^2 + \lambda \left( \alpha \sum_{j=1}^{p} \beta_j^2 + (1-\alpha) \sum_{j=1}^{p} |\beta_j| \right) \right\}$$

> Then the response value is fitted as follows:  $\hat{y} = [\hat{y}_L, \hat{y}_U]$ 

 $\hat{y}_L = (\mathbf{x}_L)^T \hat{\beta}^{\mathbf{NET}}$  and  $\hat{y}_U = (\mathbf{x}_U)^T \hat{\beta}^{\mathbf{NET}}$ where  $(\mathbf{x}_L)^T = (1, a_1, \dots, a_p), (\mathbf{x}_U)^T = (1, b_1, \dots, b_p).$ 



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- **Elastic Net** Center and Range Method
  - > Then the <u>center</u> least square estimate of  $\beta$  is obtained solving the following optimization problem:

$$\hat{\beta}^{c^{\text{NET}}} = \operatorname{argmin}_{\beta} \left\{ \sum_{i=1}^{N} (y_i^c - \beta_0 - \sum_{j=1}^{p} x_{ij}^c \beta_j)^2 + \lambda \left( \alpha \sum_{j=1}^{p} \beta_j^2 + (1-\alpha) \sum_{j=1}^{p} |\beta_j| \right) \right\}$$

> Then the <u>range</u> least square estimate of  $\beta$  is obtained solving the following optimization problem:

$$\hat{\beta}^{r^{\text{NET}}} = \operatorname{argmin}_{\beta} \left\{ \sum_{i=1}^{N} (y_i^r - \beta_0 - \sum_{j=1}^{p} x_{ij}^r \beta_j)^2 + \lambda \left( \alpha \sum_{j=1}^{p} \beta_j^2 + (1-\alpha) \sum_{j=1}^{p} |\beta_j| \right) \right\}$$



## **Elastic Net** Center and Range Method

> Then the response value is fitted as follows:  $\hat{y} = [\hat{y}_L, \hat{y}_U]$ 

$$\hat{y}_L = \hat{y}^c - \hat{y}^r$$
 and  $\hat{y}_U = \hat{y}^c + \hat{y}^r$ ,  
where  $\hat{y}^c = (\tilde{x}^c)^T \hat{\beta}^{c^{\mathbf{NET}}}$  and  $\hat{y}^r = (\tilde{x}^c) \hat{\beta}^{r^{\mathbf{NET}}}$ 

➤ The optimal value of λ is computed using Cross-Validation:





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	developers	Email oldemar.rodriguez@promidat.com
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	business, you can host and review code,	Use at least one letter, one numeral, and seven characters.
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#### E README.md

### **RSDA**

Symbolic Data Analysis (SDA) was proposed by professor Edwin Diday in 1987, the main purpose of SDA is to substitute the set of rows (cases) in the data table for a concept (second order statistical unit). This package implements, to the symbolic case, certain techniques of automatic classification, as well as some linear models.

### Installation

You can install RSDA from github with:

# install.packages("devtools")
devtools::install\_github("PROMiDAT/RSDA")

### Examples

data(ex1\_db2so) ex1\_db2so

	state	sex	county	group	age	
1	Florida	M	2	6	3	
2	California	F	4	3	4	
3	Texas	Μ	12	3	4	
4	Florida	F	2	3	4	
5	Texas	м	4	6	4	
6	Texas	F	2	3	3	
7	Florida	м	6	3	4	



### You can get this presentation at:

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Thank you.....